

## F04LHF – NAG Fortran Library Routine Document

**Note.** Before using this routine, please read the Users' Note for your implementation to check the interpretation of bold italicised terms and other implementation-dependent details.

### 1 Purpose

F04LHF calculates the approximate solution of a set of real linear equations with multiple right-hand sides,  $AX = B$  or  $A^T X = B$ , where  $A$  is an almost block-diagonal matrix which has been factorized by F01LHF.

### 2 Specification

```

SUBROUTINE F04LHF(TRANS, N, NBLOKS, BLKSTR, A, LENA, PIVOT, B,
1          LDB, IR, IFAIL)
INTEGER    N, NBLOKS, BLKSTR(3,NBLOKS), LENA, PIVOT(N),
1          LDB, IR, IFAIL
  real    A(LENA), B(LDB,IR)
CHARACTER*1 TRANS

```

### 3 Description

The routine solves a set of real linear equations  $AX = B$  or  $A^T X = B$ , where  $A$  is almost block-diagonal.  $A$  must first be factorized by F01LHF. F04LHF then computes  $X$  by forward and backward substitution over the blocks.

### 4 References

- [1] Diaz J C, Fairweather G and Keast P (1983) Fortran packages for solving certain almost block diagonal linear systems by modified alternate row and column elimination *ACM Trans. Math. Software* **9** 358–375

### 5 Parameters

- 1:** TRANS — CHARACTER\*1 *Input*  
*On entry:* TRANS specifies the equations to be solved as follows:  
     if TRANS = 'N' or 'n', solve  $AX = B$ ;  
     if TRANS = 'T' or 't', solve  $A^T X = B$ .
- 2:** N — INTEGER *Input*  
*On entry:*  $n$ , the order of the matrix  $A$ .  
*Constraint:*  $N > 0$ .
- 3:** NBLOKS — INTEGER *Input*  
*On entry:* the total number of blocks of the matrix  $A$ , as supplied to F01LHF.  
*Constraint:*  $0 < \text{NBLOKS} \leq N$ .
- 4:** BLKSTR(3,NBLOKS) — INTEGER array *Input*  
*On entry:* information which describes the block structure of  $A$ , as supplied to F01LHF.
- 5:** A(LENA) — *real* array *Input*  
*On entry:* the elements in the factorization of  $A$ , as returned by F01LHF.

- 6:** LENA — INTEGER *Input*  
*On entry:* the dimension of the array A as declared in the (sub)program from which F04LHF is called.  
*Constraint:*  $LENA \geq \sum_{k=1}^{NBLOKS} BLKSTR(1,k) \times BLKSTR(2,k)$ .
- 7:** PIVOT(N) — INTEGER array *Input*  
*On entry:* details of the interchanges in the factorization, as returned by F01LHF.
- 8:** B(LDB,IR) — *real* array *Input/Output*  
*On entry:* the  $n$  by  $r$  right-hand side matrix  $B$ .  
*On exit:*  $B$  is overwritten by the  $n$  by  $r$  solution matrix  $X$ .
- 9:** LDB — INTEGER *Input*  
*On entry:* the first dimension of the array B as declared in the (sub)program from which F04LHF is called.  
*Constraint:*  $LDB \geq N$ .
- 10:** IR — INTEGER *Input*  
*On entry:*  $r$ , the number of right-hand sides.  
*Constraint:*  $IR > 0$ .
- 11:** IFAIL — INTEGER *Input/Output*  
*On entry:* IFAIL must be set to 0, -1 or 1. For users not familiar with this parameter (described in Chapter P01) the recommended value is 0.  
*On exit:* IFAIL = 0 unless the routine detects an error (see Section 6).

## 6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors detected by the routine:

IFAIL = 1

- On entry,  $N < 1$ ,
- or  $NBLOKS < 1$ ,
- or  $IR < 1$ ,
- or  $LDB < N$ ,
- or  $N < NBLOKS$ ,
- or LENA is too small,
- or illegal values detected in BLKSTR,
- or  $TRANS \neq 'N'$  or  $'T'$ .

## 7 Accuracy

The accuracy of the computed solution depends on the conditioning of the original matrix  $A$ .

## 8 Further Comments

None.



```

READ (NIN,*)
READ (NIN,*) NBLOKS
WRITE (NOUT,*)
IF (NBLOKS.LE.NBLMAX) THEN
  NBASEK = 0
  N = 0
  DO 40 I = 1, NBLOKS
    READ (NIN,*) (BLKSTR(J,I),J=1,3)
    DO 20 K = 1, BLKSTR(1,I)
      IF (NBASEK+BLKSTR(2,I)*BLKSTR(1,I).GT.LENA) THEN
        WRITE (NOUT,*)
+         ' Array A is too small for this problem'
        STOP
      ELSE
        READ (NIN,*) (A(NBASEK+(J-1)*BLKSTR(1,I)+K),J=1,
+         BLKSTR(2,I))
      END IF
20    CONTINUE
    NBASEK = NBASEK + BLKSTR(2,I)*BLKSTR(1,I)
    N = N + BLKSTR(1,I)
40    CONTINUE
  IF (N.GT.NMAX) THEN
    WRITE (NOUT,*) ' N is too large'
    STOP
  END IF
  TOL = 0.0e0
  IFAIL = -1
*
  CALL F01LHF(N,NBLOKS,BLKSTR,A,LENA,PIVOT,TOL,INDEX,IFAIL)
*
  IF (IFAIL.EQ.0) THEN
    READ (NIN,*) IR
    IF (IR.LE.IRMAX) THEN
      READ (NIN,*) ((B(I,J),I=1,N),J=1,IR)
      IFAIL = -1
*
      CALL F04LHF('N',N,NBLOKS,BLKSTR,A,LENA,PIVOT,B,LDB,IR,
+      IFAIL)
*
      IF (IFAIL.EQ.0) THEN
        WRITE (NOUT,*) 'Component Solution'
        DO 60 I = 1, N
          WRITE (NOUT,99999) I, (B(I,J),J=1,IR)
60        CONTINUE
      END IF
    ELSE
      WRITE (NOUT,*) ' Too many right hand sides specified'
    END IF
  END IF
  ELSE
    WRITE (NOUT,*) ' NBLOKS is invalid'
  END IF
  STOP
*
99999 FORMAT (1X,I5,6X,5F6.4)
END

```

## 9.2 Program Data

F04LHF Example Program Data

```

5          : Number of blocks
 2 4 3    : Number of rows, columns and column overlap, block 1
-1.00 -0.98 -0.79 -0.15
-1.00 0.25 -0.87 0.35          : End block 1
 4 7 4    : Number of rows, columns and column overlap, block 2
 0.78 0.31 -0.85 0.89 -0.69 -0.98 -0.76
-0.82 0.12 -0.01 0.75 0.32 -1.00 -0.53
-0.83 -0.98 -0.58 0.04 0.87 0.38 -1.00
-0.21 -0.93 -0.84 0.37 -0.94 -0.96 -1.00          : End block 2
 5 8 2    : Number of rows, columns and column overlap, block 3
-0.99 -0.91 -0.28 0.90 0.78 -0.93 -0.76 0.48
-0.87 -0.14 -1.00 -0.59 -0.99 0.21 -0.73 -0.48
-0.93 -0.91 0.10 -0.89 -0.68 -0.09 -0.58 -0.21
 0.85 -0.39 0.79 -0.71 0.39 -0.99 -0.12 -0.75
 0.17 -1.37 1.29 -1.59 1.10 -1.63 -1.01 -0.27          : End block 3
 3 6 3    : Number of rows, columns and column overlap, block 4
 0.08 0.61 0.54 -0.41 0.16 -0.46
-0.67 0.56 -0.99 0.16 -0.16 0.98
-0.24 -0.41 0.40 -0.93 0.70 0.43          : End block 4
 4 5 0    : Number of rows, columns and column overlap, block 5
 0.71 -0.97 -0.60 -0.30 0.18
-0.47 -0.98 -0.73 0.07 0.04
-0.25 -0.92 -0.52 -0.46 -0.58
 0.89 -0.94 -0.54 -1.00 -0.36          : End block 5
 1          : Number of right hand sides
-2.92 -1.27 -1.30 -1.17 -2.10 -4.51 -1.71 -4.59
-4.19 -0.93 -3.31 0.52 -0.12 -0.05 -0.98 -2.07
-2.73 -1.95          : End right hand side 1

```

## 9.3 Program Results

F04LHF Example Program Results

Component Solution

```

 1      1.0000
 2      1.0000
 3      1.0000
 4      1.0000
 5      1.0000
 6      1.0000
 7      1.0000
 8      1.0000
 9      1.0000
10      1.0000
11      1.0000
12      1.0000
13      1.0000
14      1.0000
15      1.0000
16      1.0000
17      1.0000
18      1.0000

```